



## INTRODUCTION

From an experimental point of view, single-electron transfer has at least two interesting facets. First, it can be used as a tool for spectroscopy. Energy gain spectroscopy and the related experiments in inverse kinematics which exploit the recoil ion longitudinal momentum for  $Q$ -value determination (change in the electron binding energies) give access to the energy levels of highly charged species and to energy levels that do not decay radiatively. These are difficult to access by other spectroscopic techniques. Second, the dynamics of the transfer process itself is of fundamental interest since it combines electron-electron dynamics, correlation, and questions of few-body momentum exchange.

In most of the theoretical studies the transfer into an excited state or the transfer combined with a target excitation of a second electron were neglected. Especially at higher impact energies  $E_p > 100$  keV/u, where the final state determination in experiments are difficult, the influence of excitation has not been investigated. Nowadays the modern experimental technique of COLTRIMS (Cold Target Recoil Ion Momentum Spectroscopy) allows to measure the final electronic states in electron transfer reactions even at high impact energies.

We consider here the transfer reaction  $p+\text{He} \rightarrow \text{H}+\text{He}^+$  at different high proton energies and present both the experimental single differential cross sections for total excitation of the residual helium ion ( $n \geq 2$ ), and the calculations within first Born approximation (FBA).

## EXPERIMENT

For the swift collisions investigated here, the best resolution is obtained by detecting the recoil ion momentum instead of small change on the large projectile momentum. In the present experiments we have used the COLTRIMS technique to measure both the neutral projectile  $\text{H}_0$  and the recoil ion  $\text{He}^+$  in coincidence [1, 2]. The experiment has been performed at the 2.5 MV van de Graaff accelerator at the Institut für Kernphysik, University of Frankfurt. We used two sets of adjustable slits to collimate the beam to a size of  $0.5 \times 0.5$  mm<sup>2</sup> at the target. Two sets of electrostatic deflectors are placed in front and behind the target. They were used to clean the beam from charge state impurities in front of the target and to analyze the final charge state behind the target. The neutral  $\text{H}_0$  projectiles were detected on a 40-mm position- and timesensitive multichannel plate (MCP) detector with delay line anode for position read-out [3]. The target is provided by a 2-stage supersonic gas jet. At the interaction point, the gas jet has a diameter of 1.5 mm and areal density of  $5 \times 10^{11}$  atoms/cm<sup>2</sup>. The  $\text{He}^+$  recoil ions produced in the overlap region of gas jet and projectile beam were projected with a weak electrostatic field (4.8 V/cm) onto a 80-mm position- and time-sensitive multi channel plate detector. A three-dimensional time- and space focusing geometry was applied to maximize the resolution [4]. From the measured data, time of flight (19  $\mu\text{s}$  for  $\text{He}^+$ ) and position of impact, we extracted the initial three-dimensional momentum vector. We achieved an overall momentum resolution of 0.1 a.u. which was limited by the target temperature. Our spectrometer geometry and electric fields yielded  $4\pi$  acceptance angle for all recoil ions with momenta below 9 a.u.

In the plane perpendicular to the beam axis, we measure the scattering angle of the projectile and the transverse momentum of the recoiling ion. By momentum conservation they must add to zero. We used this for background suppression. We deduced the scattering angle from the recoil ion transverse momentum, which has a much better momentum resolution in our setup. By gating on the different longitudinal momenta of the recoil ion, we were able to extract the scattering angles for different final electronic states [5]. The small background contribution, mainly from single ionization, has been subtracted.

## THEORY

Let us denote the projectile proton momentum by  $\vec{p}_p$ , the hydrogen momentum by  $\vec{p}_H$ , and the recoil-ion momentum by  $\vec{K}$ . We also define the transferred momentum as  $\vec{q} = \vec{p}_H - \vec{p}_p$ . We can deduce its approximate value using the momentum and energy conservation

$$\vec{q} + \vec{K} = 0, \quad (1)$$

$$\frac{p_p^2}{2m} + E_0^{\text{He}} = \frac{p_H^2}{2(m+1)} + \frac{K^2}{2M} + E^H + E^{\text{ion}}. \quad (2)$$

Here  $\vec{K}$  is the ejected electron momentum, the proton mass  $m = 1836.15$ , the helium ion mass  $M \approx 4m$ ,  $E_0^{\text{He}} = -2.903724377034$ . Now we choose very small scattering angles for the outgoing hydrogen ( $0 \leq \theta_p \lesssim 0.5$  mrad). It leads to a practically zero ion velocity  $K/M$  in the laboratory frame during the process, and we can consider the ion like immovable. The proton velocity  $\vec{v}_p = \vec{p}/m$  varies about a few a.u. for its energy of several hundredths keV. This fact allows one to neglect  $K^2/2M$  and  $q^2/2m$  after insertion of  $\vec{p}_H = \vec{q} + \vec{p}_p$  into eq. (2). As a result we obtain

$$\vec{v}_p \vec{q} = \frac{1}{2} v_p^2 + Q; \quad Q = E_0^{\text{He}} - E^H - E^{\text{ion}}, \quad (3)$$

## THEORY

and choose the vector  $\vec{v}_p$  as  $z$ -axis; there follows the longitudinal component  $q_z = v_p/2 + Q/v_p$ . The transverse component of the vector is  $\vec{q}_\perp = (\vec{p}_H)_\perp \approx m v_p \theta_p$ .

We have two types of single differential cross section (SDCS) for TE processes:

$$\frac{d\sigma^{(1)}}{d\theta_p} = \frac{m^2 \theta_p}{(2\pi)} \sum_{n=2}^{n-1} \sum_{l=0}^l \sum_{m=-l}^l |T_{nlm}^{\text{FBA}}|^2 \quad (4)$$

and

$$\frac{d\sigma^{(2)}}{d\Omega_p} = \frac{m^2}{(2\pi)^2} \sum_{n=2}^{n-1} \sum_{l=0}^l \sum_{m=-l}^l |T_{nlm}^{\text{FBA}}|^2 \quad (5)$$

We omit in short the mathematical details of description of the symmetrized matrix elements  $|T_{nlm}^{\text{FBA}}|$ , which are given in [6, 7]. We calculate them with use of 3D and 4D integrals.

In theoretical calculations we use four trial ground-state helium wave functions. One is the loosely correlated  $1s^2$  Roothaan-Hartree-Fock (RHF) wave function [8] (no angular correlation) with a rather poor ground-state energy of  $E_{\text{He}}^{\text{RHF}} = -2.8617$  a. u. Second one [9] includes angular correlations, but its ground energy is also far from the experiment  $E_{\text{He}}^{\text{SPM}} = -2.8952$ . Two another trial functions are highly correlated ones. It is given in [10] with a ground-state energy of  $E_{\text{He}}^{\text{Chu}} = -2.903721$  a. u. and that of Mitroy [11] with  $E_{\text{He}}^{\text{Mitroy}} = -2.9031$ . Their energies are very close to the experimental value.

## RESULTS AND DISCUSSION

In Figs. 1,2,3 and 4 we present experimental and theoretical SDCS1.

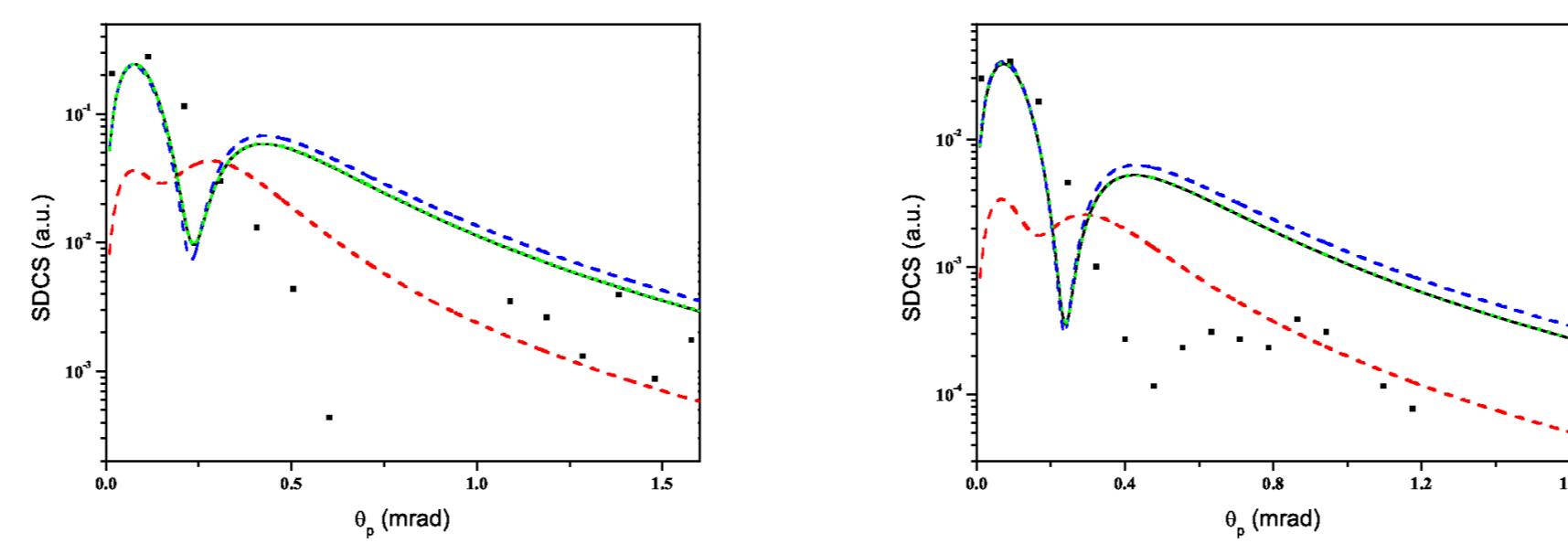


Figure 1: Experimental and theoretical data for  $E_p = 630$  keV (left panel) and  $E_p = 1000$  keV (right panel)  $p+\text{He}$  collisions and  $\theta_p \leq 1.5$  mrad. Full squares is the experiment, red line the RHF [8] trial helium wave function, blue line SPM [9], black [10] and green [11] practically coincide.

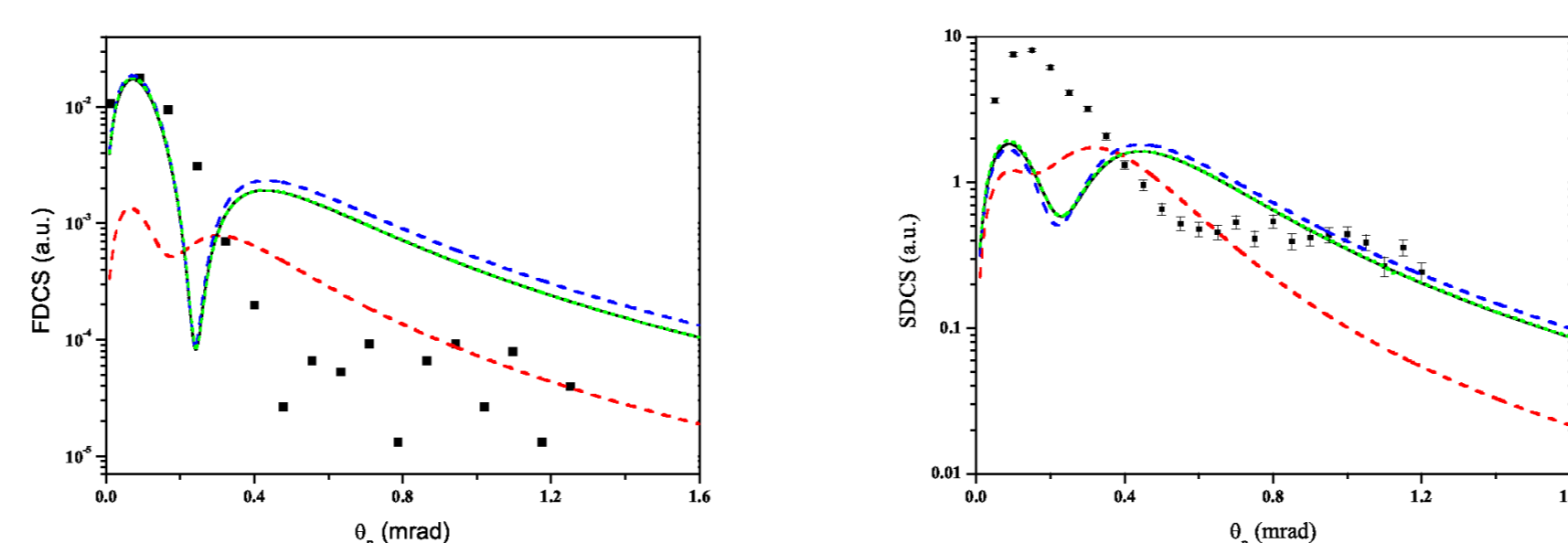


Figure 2: The same like in Fig.1, but  $E_p = 1200$  keV (left panel) and  $E_p = 300$  keV (right panel).

The shape of the SDCS1 is formed by three FBA terms, one of which (OBK) provides the direct  $\text{He} \rightarrow e+\text{He}^+$  decay mechanism, and two others provide the double decay of the helium in the intermediate state  $\text{He} \rightarrow 2e+\text{He}^{2+}$ . The absolute value of the cross sections is about 1% of that when the residual ion stays in its ground state (charge transfer, CT), and the shape in the case of helium wave functions with angular correlations has the minimum and reminds the case  $n = 1$  [7]. The wave function without angular correlations fails at all. It is interesting to note, that FBA SDCS1 for CT reactions practically does not depend on the trial helium wave function, and even the simplest  $1s^2$  one describes well the main peak.

We also see that  $E_p \sim 500$  keV is the boundary energy when FBA still describes somehow the main peak at very small  $\theta_p$ . The FBA also fails to describe the position of the minimum and the behavior of the cross section beyond it. We need to attract here the SBA or DWBA calculations.

We have to work out at least computer code for 9D integration to

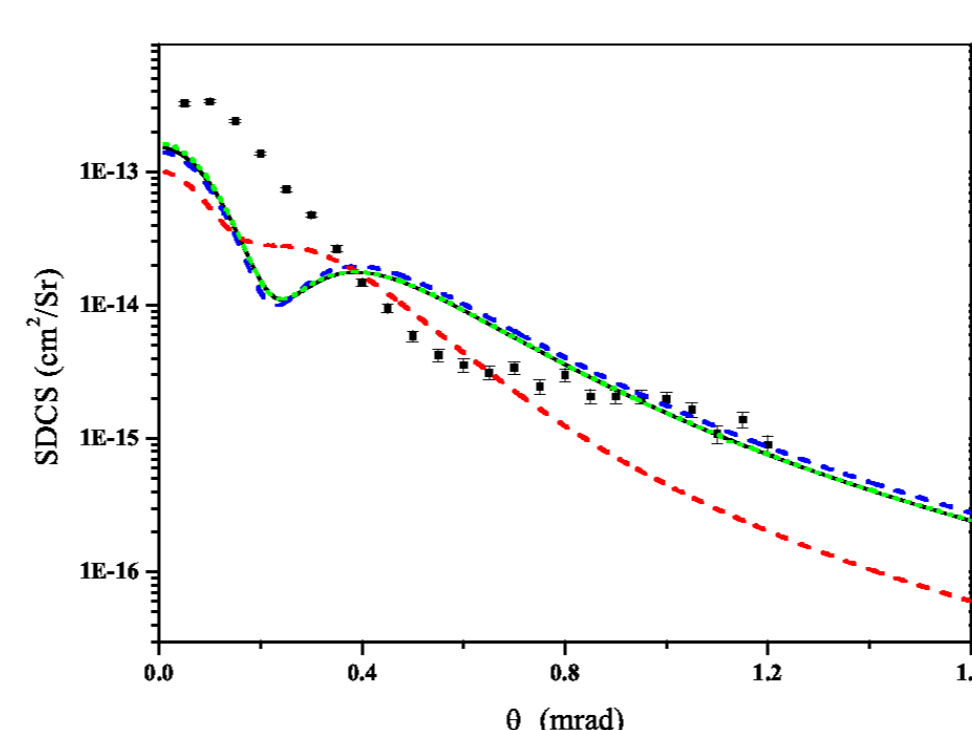


Figure 3: SDCS2 calculations versus the scattering angle  $\theta_p$ . Colors of curves are the same like in Fig.1.  $E_p = 300$  keV,  $n = 2 + 3$ .

## RESULTS AND DISCUSSION

calculate the SBA or DWBA. Such the FBA calculations of the SDCS2 are presented in [12] for  $E_p = 300$  keV, but the result was about 150 times bigger than the experiment. Our correct results on the base of 9D calculations are presented for the first time in Fig. 3. They quite coincide with both 3D calculations and the experiment ( $n = 2 + 3$ ). See also our discussion in [13, 14]. Useful to note that

$$\sum_{n=1}^{n-1} \sum_{l=0}^l \sum_{m=-l}^l |T_{nlm}|^2 = \int \frac{d^3k}{(2\pi)^3} |\langle \vec{k} | T \rangle|^2 - \int \frac{d^3k}{(2\pi)^3} |\langle \varphi^-(\vec{k}) | T \rangle|^2. \quad (6)$$

Here  $\langle \varphi^-(\vec{k}) | T \rangle$  is the transfer ionization (TI) amplitude of the reaction considered, and  $\langle \vec{k} | T \rangle$  is the same but the coulomb wave is replaced by the plain wave. This is another way to calculate the total sum by excited states.

Next, we calculate 9D integral with the eikonal phase-factor obtained earlier in [7]

$$T_{nlm}^{\text{DWBA}} \approx \sqrt{2} \int d^3R e^{-i\vec{R}\vec{q}} \int d^3\rho e^{i\vec{\rho}\vec{v}_p} \varphi_0(\rho) \int d^3r_2 \phi_{nlm}^*(\vec{r}_2) \times e^{[-i/v_p f(\vec{R}, \vec{\rho}, \vec{r}_2)]} \left[ \frac{1}{\rho} - \frac{1}{|\vec{R} - \vec{r}_2|} + \frac{2}{R} \right] \Phi_0(\vec{R} - \vec{\rho}, \vec{r}_2). \quad (7)$$

with

$$f = \ln \left[ \frac{[v_p |\vec{R} - \vec{\rho}| + \vec{v}_p \cdot (\vec{R} - \vec{\rho})] [v_p |\vec{R} - \vec{r}_2| + \vec{v}_p \cdot (\vec{R} - \vec{r}_2)]}{[v_p R + \vec{v}_p \cdot \vec{R}] [v_p |\vec{R} - \vec{\rho} - \vec{r}_2| + \vec{v}_p \cdot (\vec{R} - \vec{\rho} - \vec{r}_2)]} \right]$$

This phase-factor is a part of the SBA, and can be considered like modified 4C approximation (in analogy to 3C and 6C). Results for  $E_p = 630$  and 1000 keV are presented in Fig. 4. We see positive evaluation of the main peak towards the experiment. However, this DWBA can not improve the situation at bigger scattering angles, and full SBA calculations are needed.

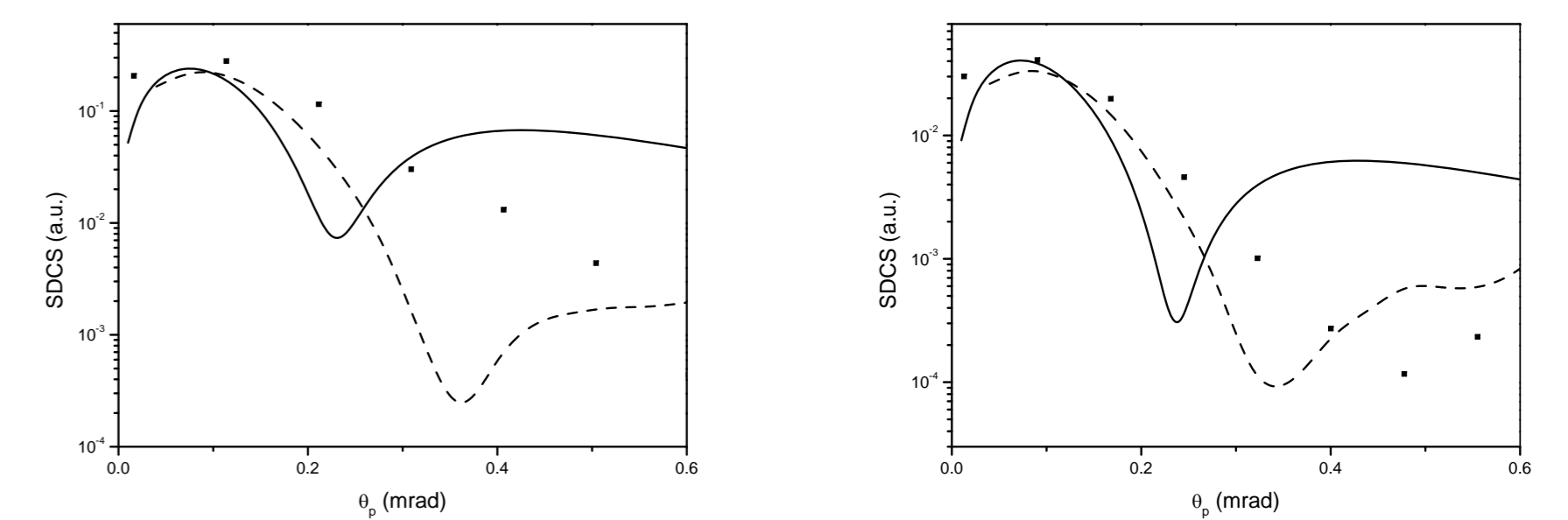


Figure 4: SDCS1 calculations versus the scattering angle  $\theta_p$ . SPM FBA calculations are supplemented by the phase factor. Solid line: SPM, dashed line: SPM with the 4C phase factor,  $n = 2 + 3$ . Left panel,  $E_p = 630$  keV. Right panel,  $E_p = 1000$  keV.

## CONCLUSION

In conclusion, we present the SDCS experimental data and FBA theory for transfer excitation proton-helium collision at 300, 630, 1000 and 1200 keV/u. In calculations both  $1s^2$  and highly correlated trial helium wave functions are used. The  $1s^2$  wave function fails to describe the experiment, while angular correlated functions give practically coincident results and well reproduce the experiment in a vicinity of main peak. 300 keV/u results show the limit for the FBA theory. Also 3D and 9D calculations give coincident results, close to the experiment.

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